

**MATH 467 FACTORIZATION AND PRIMALITY
TESTING, FALL 2025, PROBLEMS 13**

Return by Monday 1st December

Submit any code you write to answer these questions.

1. For each number below

(i) $n = 37038381852397$,

(ii) $n = 1543267864443420616877677640751301$,

(iii) $n = 23456789023456789923456789923454566777888990189$,

(iv) $n = 2447952037112100847479213118326022843437705003126289$,

(v) $n = 59545797598759584957498579859585984759457948579595794859456799501$,

list the odd primes $p \leq 200$ for which n is a quadratic residue modulo p .

2. Let n be as in (i) above. List the x with $6085000 \leq x \leq 6087000$ for which $|x^2 - n|$ completely factorises into primes $p \leq 200$ and in each case give the factorisation.